

Mathematics Policy and Protocol

Written: May 2020 Reviewed: Sept 2023 Next review: Sept 2024

Principle Academy Vision

The Pioneer Academy promotes and achieves excellence by ensuring the very best care and guidance for every child within our family of schools. It recognises the importance of outstanding teaching and learning by actively encouraging creativity and innovation, whilst having consistent standards of behaviour and attendance. Treating everyone as equal, whilst celebrating diversity, is a non-negotiable; protecting all through safeguarding, health and safety and welfare is paramount.

Introduction

This document is a statement of the aims, principles and strategies for the teaching, learning and assessment of mathematics at The Pioneer Academy Schools. We believe every child can do maths. Our aim is to facilitate highly effective teaching and learning that is practical, challenging and engaging, whilst supporting children on their journey towards mastery. Every adult has the highest expectations of the children, and as such, expects all children to attain high standards. Children are expected to develop a deep understanding of a concept through mathematical reasoning before progressing to the next level.

Philosophy

The new National Curriculum states that:

"Mathematics is a creative and highly inter-connected discipline that has been developed over centuries, providing the solution to some of history's most intriguing problems. It is essential to everyday life, critical to science, technology and engineering, and necessary for financial literacy and most forms of employment.

A high-quality mathematics education therefore provides a foundation for understanding the world, the ability to reason mathematically, an appreciation of the beauty and power of mathematics, and a sense of enjoyment and curiosity about the subject."

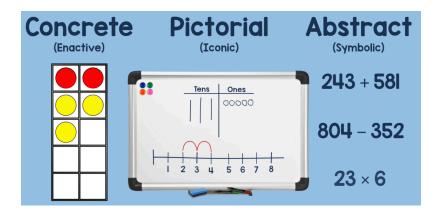
At The Pioneer Academy we see Maths very much as a multi-discipline, cross curricular, interconnected subject which encourages creativity. We believe that talking and reasoning about Maths is as important as performing calculations. We want the children to see Mathematics as being relevant to their world and applicable to everyday life as well as being something that they will need as they move on through their school life and ultimately to the world of employment. Their learning experience should be one that develops the children's ability to think mathematically and one which allows them to apply the knowledge, understanding and skills they have learned in a variety of ways

The National Curriculum identifies three main aims in the primary phase:

- become fluent in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately.
- reason mathematically by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language

• can solve problems by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions

At The Pioneer Academy Schools we aim to ensure that conceptual, pictorial, and abstract (CPA) understanding is integrated into lessons alongside procedural and factual fluency. We believe that maths does not rely on rote learning of facts and procedures without the underlying understanding required to use them effectively. There is a focus on number and calculation from the beginning.



We aim to promote positive attitudes towards maths as we believe there is a link between success, confidence and enjoyment. We achieve this is by the use of maths across the curriculum and by making maths fun.

Scheme of Work

We follow <u>White Rose Maths (WRM)</u>. This is a mastery approach to the teaching of Mathematics whereby topics are taught in depth over a longer period. This allows for the mastering of concepts before moving on to the next sequence. This we believe paves the way for children to be secure in what they have learnt. Click <u>here</u> to access the WRM progression document.

Calculation Policy

We follow the White Rose Calculation Policy which introduces key concepts using a concrete-pictorial-abstract approach. (See separate document)

Planning

Teachers in all year groups plan using the White Rose scheme as the basis for most of their work, supplemented with resources such as <u>Premium WRM</u>, <u>Rising Stars</u>, <u>Classroom Secrets</u> or <u>Twinkl (Dive into Master)</u>. We aim, wherever possible, for children to access the work from their own year group. Occasionally, there may be a small number of children for whom this is not appropriate. They will look at earlier year groups if this is the case. Higher Ability children are extended using additional reasoning resources, maybe from <u>NRich</u> or <u>NCETM</u> etc.

Planning a Lesson

When planning a lesson, teachers need to plan for a balance of conceptual understanding, language and communication and mathematical thinking to support children's mathematical problem solving. If a pupil has meaningful understanding of the maths they are learning, they will be able to represent it in different ways, use mathematical language to communicate related ideas and think mathematically with the concept. This will enable them to apply their understanding to a new problem in an unfamiliar situation.

Engaging with WRM Schemes of Work

1. Get an overview of the block

• What should pupils be able to understand and apply by the end of this block?

- How does the block progress?
- What is the key learning which needs to be covered?
- Are there links to previous/future learning?

2. **Consider the key teaching points** - these will need to be reinforced throughout the block.

- What needs to be modelled and how to the children? How will you model this alongside the calculation? •
- What are the key sentence structures and vocabulary? (See Appendices 4 and 5)
- What are the small steps for the learning?
- What concrete, pictorial and abstract representations would be most appropriate during the block? •
- What misconceptions will need to be addressed or anticipated? •
- What questions will promote a deeper understanding of the concepts taught? (See Appendix 2)

3. Decide how the unit will need to be adapted for your class

- How will you differentiate? How will you scaffold? Will you use constraints? (See Appendix 3) •
- How will you promote learning for depth? What opportunities for reasoning will you include? How might you use • conceptual/procedural understanding? (See Appendix 1)
- Will any pre-teaching be required? Would it be most useful to use consolidation lessons- at the • beginning/end/middle of block?
- Will more/less time be needed on certain key learning?
- What are my expectations of how pupils will progress?
- What sharing strategies might pupils in use; Use manipulatives, create visual images, guesstimate (trial and error), • work backwards, look for a pattern, create a systematic list, create a table...

Teaching

- Lessons can be structured in a variety of ways to suit the topic and the class. Example A: Do Now, New Learning, Talk Task, Develop Learning, Independent Task, Plenary Example B: Discover, Share, Think Together, Practise, Reflect Example C: Continuation from previous lesson
- Whole class teaching is used only when appropriate.
- The children get the opportunity for collaborative work and independent work.
- There are five maths lessons a week. In Key Stage 1 teachers ensure that every child undertakes mathematical • activities for at least 40 minutes per day. In Key Stage 2 daily mathematics lessons are at least an hour long.
- Key vocabulary for the lesson is taught and displayed. Full sentence responses are modelled and expected.
- The use of worksheets for children's work is discouraged. However, learning prompts, scaffold or frames can be used • to support learning.
- The following **core representations** or manipulatives are used across the school: ٠

	Place Val	ue charts	Money	Part-whole models
	Arrays		Base 10	Bar models
	Numicon		Cuisenaire rods	Tens frames
	Place	Value	Bead strings	
Counters			Number lines	

C

- A Working Wall and maths displays are used to support learning.
- Teachers plan for other opportunities for the preview and review of learning; Daily Ten, Maths Meetings, TT Rockstars, MyMaths, Maths with Parents, Big Maths, Flashback Four, True or False.....

Early Years

We aim daily for short adult-led focused inputs which can either be for the whole class or groups. This does not have to be formal and can include number rhymes, songs, and games as well as suggested prompts for learning from WRM. The children also have regular opportunities to practise their counting and subitising skills and revisit prior learning.

These inputs can be followed up with short adult-led activities 2/3 times each week. Opportunities to practise new skills through play are encouraged in different areas of the provision either independently or with adult support.

<u>Assessment</u>

- Regular moderation staff meetings are planned throughout the year to ensure consistency in teacher assessments across the school.
- Gaps in learning will be identified on a regularly basis and children will be given targeted intervention time before the next lesson to enable them to move on with the rest of the class. WRM End of Block and End of Term Assessments are used for this purpose.
- Interventions are provided to boost children's progression in maths.

Computing

Opportunities to use computing to support teaching and learning are planned for and used as appropriate.

Appendix 1 – Depth of Understanding

<u>All</u> pupils should be given opportunities to deepen their understanding. Pupils are less likely to consolidate understanding of a concept if they have only a simple, procedural understanding of it that relies heavily on limited representations with no connections to familiar ideas or contexts. Consider how you can support deeper understanding throughout the lesson...

'What's the question?' If this is the answer, what could the question have been? This could be an equation or a word problem.	'Reason it' Explain to your partner how you know. Remember to use the star words!	'What's wrong with this?' Can you explain what is wrong with this and correct the error?
'What's the same? What's different?' Can you find anything that is the same about these two numbers/shapes/calculations? Now can you find something that is different?	'Find a pattern' Can you see a pattern (in the numbers)? Can you see a pattern in the answers? Continuing this pattern, what would happen if? What came before? What comes next? Explain how you know	'Have you found all possibilities?' Is there more than one way of completing this? Is there more than one answer? Have you found them all?
'Draw it' Draw a picture to explain or demonstrate what you have worked out	Hedging It <u>must</u> be It <u>could</u> be It <u>can't</u> be	'Maths story' Make up a real-life story using your equation/numbers or shapes. Try to use the star words.
How do you know? Why do you know? Explain why	'Show me!' Convince me that you are right.	True/False/Always, Sometimes, Never True

Reasoning Skills

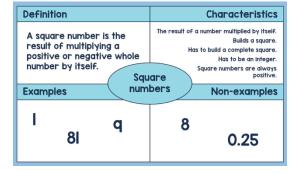
Describing	Simply tells what they did
Explaining	Offers some reasons for what they did (may or may not be correct)
Convincing	Confident that their chain for reasoning is right (inductive reasoning)
Justifying	A correct logical argument that has a complete chain of reasoning
Proving	A watertight argument that is mathematically sound (deductive reasoning)

Thinking Through Variation (What do we want them to think about? Not what do we want them to do)

Conceptual Variation	Procedural Variation	
Examples a	nd	Spotting patterns
Non-Examples		Making Connections
Standard and Non-Standar	rd	Generalisations

This allows us to...

- Strengthen children's understanding
- Generalise a concept
- Ensure they are thinking carefully and deeply



Frayer Model

Appendix 2 – Questioning

The questions and prompts that we ask, both those that are planned, and those that we improvise in the moment, are crucial in supporting pupils' developing mathematical thinking.

Exemplifying	Give me one or more examples of
Specialising	Describe (show, choose, draw, find,) an example of
	Is an example of?
	What makes an example?
	Find a counter-example of?
Completing	What must be added/removed/altered in order to allow/ensure/contradict?
Deleting	What can be added/removed/altered without affecting?
Correcting	What needs to be changed so that?
	Tell me what is wrong with
Comparing	What is the same and what is different about?
Sorting	ls it or is it not?
Organising	Sort or organise the following according to
Changing	Change in response to imposed constraints.
Varying	What if?
Reversing	Do in two (or more) ways. What is quickest, easiest,?
Altering	If this is the answer to a similar question, what was the question?
	Alter an aspect of something to see the required effect.
Generalising	What happens in general?
Conjecturing	Of what is this a special case?
	ls it always, sometimes, never?
	Describe all possible as succinctly as you can.
	What can change and what has to stay the same so that is still true?
Explaining	Explain why
Justifying	How is used in? Explain the role or use of
Verifying	Give a reason (using or not using).
Convincing	How can you be sure that?
Refuting	Convince me that
	Tell me what is wrong with
	Is it ever false that? (Always true that?)

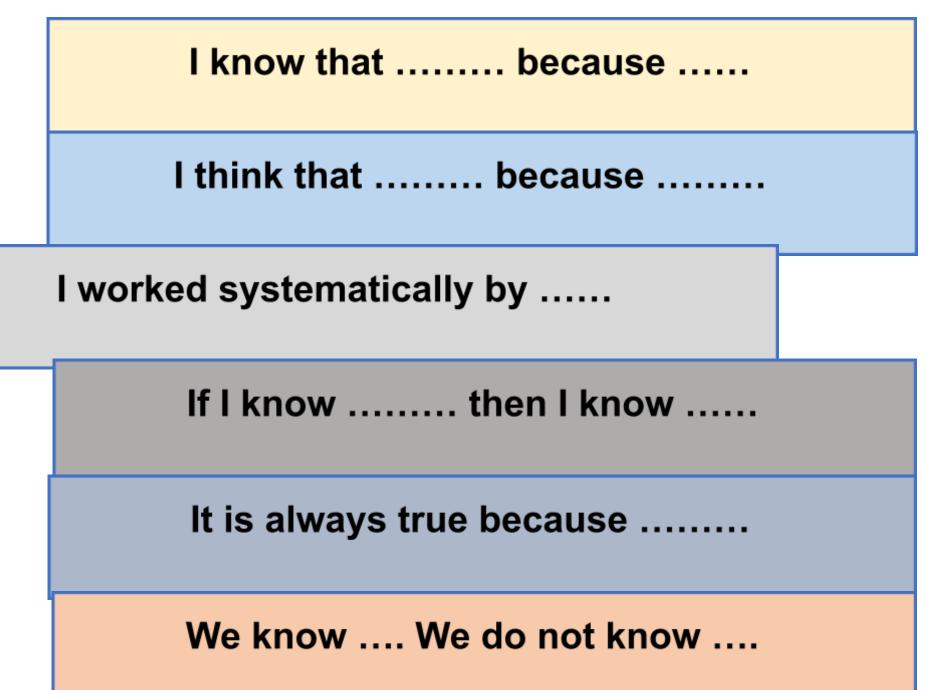
Ongoing adapt or vary - questioning			
Mathematical Thinking	Conceptual Understanding	Language and Communication	
CompareWhat do you notice?	Compare What do you notice?	Why do you think that? How	
What's the same? What's	What's the same? What's	would you? Explain your	
different?	different?	choices.	
When might this be useful? What	Can you represent this in a	Can you explain a different way	
maths that we know is this similar	different way? Do you know	that you know this? What have	
to?	another word for that?	you discovered?	
Can you group these? How many	Which is the odd one out? Why?	Is this always true, sometimes true	
ways can you find?	Can you give me another example	or never true?	
Have you found all possibilities?	of? And another?		
How do you know? What if (we	Can you give me an obvious		
change)?	example of? Can you give me an		
	unusual example of?		

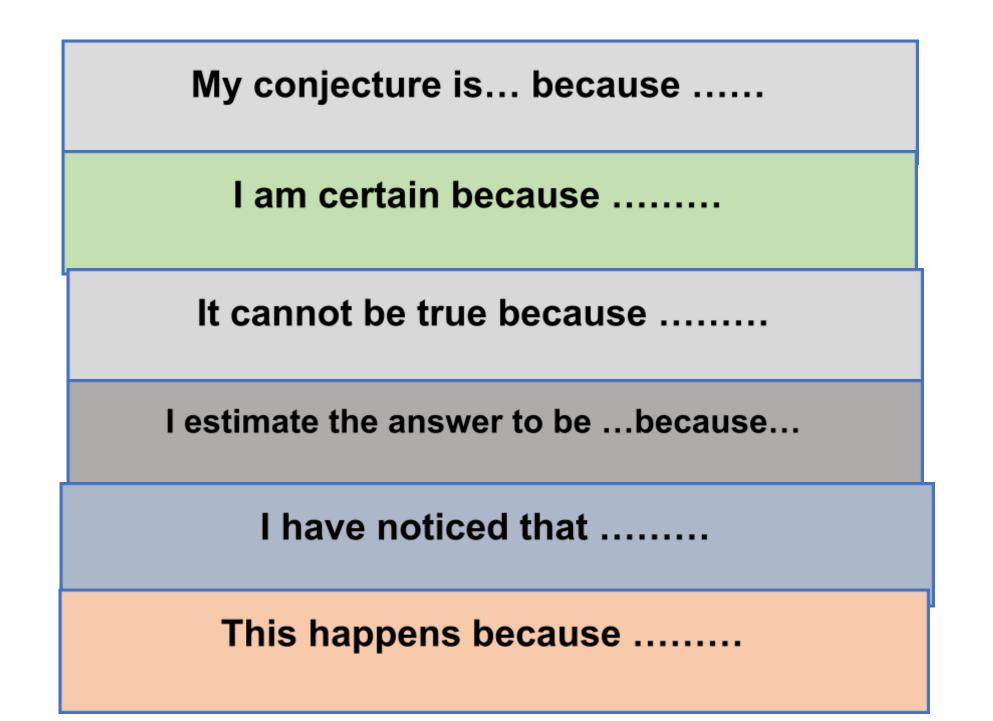
Techniques to Extend

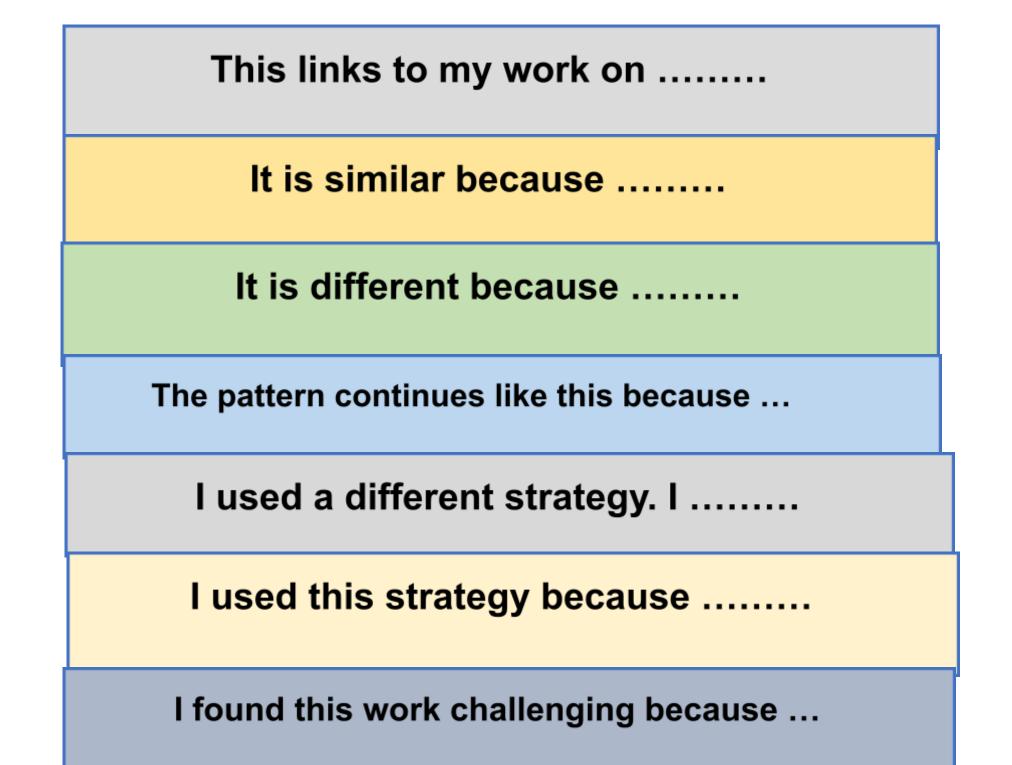
- Remove different information
- Remove 2 pieces of information and give constraints
- Interleave previously taught skills
- Use multiple representations to explain their answers (including concrete and pictorial)
- Spot patterns, make connections
- Create your own question

Techniques to Enable

- Pictures to match the problem
- Manipulatives to represent the problem
- Additional questions or hints as a way into the problem
- Pictorial representations, such as a bar model, to understand the operations needed
- Stem sentences







<u> Appendix 5 – Key Vocabulary</u>

These words should be shared meaningfully with the whole class at (or before) the start of the lesson. As well as all pupils repeating them, teachers should ensure that pupils develop understanding of each word, making use of appropriate representations (concrete or pictorial) and / or contexts that are familiar. The intention is for all pupils to use this key vocabulary accurately throughout the lesson.

The vocabulary listed here is vocabulary that pupils are expected to use and understand on a daily basis within that year group, though the definitions are written for teacher reference and would not necessarily be shared with children as they stand. The vocabulary listed is cumulative and builds on the vocabulary previously introduced.

RECEPTION		
	Definition	Example
Above	Used to describe a higher position	The Maths Meetings board is
	than another object.	above the sink.
Add	Carry out the process of addition.	l can add two numbers together
		to find a total.
Addition	The operation to combine at least two	· · ·
	numbers or quantities to form a furthe	· ·
	number or quantity, the sum or total	I.
	Addition is the	
	inverse operation to subtraction.	
Altogether	In total.	That will be £2 altogether
		please.
Balance	A measuring tool used to weigh objects	
	It has two dishes hanging on a bar. Both	
	dishes will be level when the content weigh the same. Also, as a verb	-
	indicates equivalence and equality.	The two objects balance which
		means they have the same mass.
Before	In front of or prior to.	The number '3' comes before '5'
belote		on the number line.
Below	Used to describe a lower position that	
	another object.	board.
Between	Indicates a position in relation to two	oThe teacher is standing
	other places or objects on either side.	between two tables.
Capacity	The amount of liquid a container ca	nThis cup is full to capacity
	hold.	because it cannot hold any more
		, water.
Circle	The name of a 2-D shape. A circle has a	a
	curved side.	
Clock	A tool used to measure time.	The clock shows us that the time
		is now 2 o'clock.
Compare	Look for similarities and/or difference	sl can compare these two sets –
	between at least two objects or sets.	this set has more.

Mathematical vocabulary from Reception to Year 6

Corner	A point where two or more lines	The table has four corners
	meet. The correct mathematical term is	
	vertex (vertices).	(,
Cost	A monetary value assigned to a	This apple costs 10p. What coin
	good or service.	could I use to pay for it?
Count	Assigning one number name to each of a	counted the children in the group -
	set of objects to determine how many	there are four so we will need four
	there are.	pencils.
Cube	A 3-D shape with six identical square	
	faces.	
Cuboid	A 3-D shape with six rectangular	
	faces.	
Curved surface	A non-plane surface of a 3-D shape.	The cope has a curved surface
	Both cones and cylinders have curved	The cone has a curveu surface.
	surfaces.	
Cylinder	A 3-D shape with two circular faces	
Cymruer	joined by a curved surface.	
2-D	Abbreviation for two-dimensional. A	A square is a 2-D shape.
	figure is two-dimensional if it lies on a	
	plane.	
3-D	Abbreviation for three- dimensional.	A cylinder is a 3-D shape.
	A solid is three- dimensional and	
	occupies space.	
Describe	To express mathematical features,	Can you describe the properties
	qualities and details in words.	of a cube?
Difference		The difference between ten and six is
		four.
	by comparing the quantity of one set of	
	objects with another.	
Direction	The orientation of a line in space.	Which direction should we jump –
		forwards or backwards?
Distance	A measure between two points or	The distance between my house and
	things.	the school is longer than that
		between the school and the train
		station.
Double	To multiply by two or add a value to	Ten is double five.
	itself.	
Edge	A line segment joining two vertices of	A triangle has three edges and a cube
	a plane figure (2-D shape) and	has 12 edges .
	the intersection of two plane faces (in	
	a 3-D shape).	

Empty	Containing nothing. Most commonly used in the context of measures.	There is no more water left in the jug – it is empty .
Equal	Indicates equivalence between two values and can be expressed with the symbol '='. The symbol is read as 'is equal to' which means the same as. Expressions on either side of the symbol have the same value.	My sets are equal because there are four bears in this set and there are four bears in this set.
Face	One of the plane surfaces of a solid shape.	A cube has six faces .
Fewer	A lesser amount – used when counting discrete objects, i.e. countable objects such as, pens, teddies, counters, etc.	There are fewer buttons on my coat than yours.
First	Comes before all others in time or position.	First I brush my teeth. Then I go to bed.
Flat	A level surface.	The table has a flat rectangular surface.
Full	Contains/holds as much or as many as possible; has no empty space.	The juice carton is not full because I drank some.
Group	To make equal size groups. This is one model for division.	I will group the crayons equally so that each person gets two.
Half	One of two equal parts of a shape, quantity or object.	I have shared the dolls into two equal groups – I have half and you have half .
Intersection of sets	Where the two subsets overlap in a Venn diagram. Objects or values which belong to both subsets are placed here.	The number 4 belongs in the intersection because it is even <i>and</i> less than 5.
Last	Comes after all others in time or order.	Rory is the last person in the line.
Length	A linear measurement.	The length of my snake is shorter than yours.
Less	A smaller amount or not as much.	I have 15p and you have 7p. you have less money than me.
Line	A set of adjacent points that has length but no width.	I have drawn a line matching the number four with the four ducks.
Long	An adjective used to describe length.	I have a long piece of string.
Mass	A measure relating to the amount of matter within a given object.	The mass of the school bag is greater than the mass of the book.
Measure	To find the size of something in a given unit.	How might we measure how much flour we need to bake a cake?

Minus	A name for the symbol '-', which	Three minus one is equal to
iviirius	denotes the operation of	two.
	subtraction.	
More	A greater amount.	I have six apples and you have
		two. I have more .
Next	Comes immediately after the	The next shape in my pattern is
	present one in order.	a square.
Number bond	A pair of numbers with a given	Five and four make a number
	total.	bond to nine.
Number line	A linear, continuous representation of	This number line starts at zero and
	number. Each number occupies a point	ends at ten.
	on the line, and there is an equal	
	interval between each	
	number.	
Number track	A linear, discrete representation of	I can count from one to ten,
	number. Each number is positioned in a	moving a counter along this
	square on the track.	number track.
Order	Describes the placement of items	I have ordered the bears from
	according to given criteria or in a	smallest to biggest.
	pattern. As a verb, to place items	
	according to given criteria or in a	
	pattern.	
Pair	A set of two things used together.	Socks come in a pair – one for
		each foot.
Pattern	A systematic arrangement of	The pattern is red, blue, red,
	numbers, shapes or other elements	blue, red blue.
	according to a rule.	
Plus	The word representing the operation	Five apples plus two apples are
	of addition. It is also the	equal to seven apples.
	name for the symbol '+'.	
Rectangle	A quadrilateral with four right	
	angles.	
Second	A unit of time.	Mohsin is second in the line
	An ordinal number.	today.
Sequence	A series of numbers or other	The number 3 is next in the
•		
	elements which follow a rule.	
		sequence because each number is one less than the one before.
Set	elements which follow a rule.	sequence because each number is one less than the one before.
Set		sequence because each number is one less than the one before. I have placed all the purple
Set	elements which follow a rule. A defined group of objects,	sequence because each number is one less than the one before. I have placed all the purple counters in this set because they are
	elements which follow a rule. A defined group of objects, numbers or other elements.	sequence because each number is one less than the one before. I have placed all the purple counters in this set because they are all the same colour.
	elements which follow a rule. A defined group of objects, numbers or other elements. To distribute fairly between a given	 sequence because each number is one less than the one before. I have placed all the purple counters in this set because they are all the same colour. I will share the crayons equally
Set Share	elements which follow a rule. A defined group of objects, numbers or other elements. To distribute fairly between a given	sequence because each number is one less than the one before. I have placed all the purple counters in this set because they are all the same colour.
	elements which follow a rule. A defined group of objects, numbers or other elements. To distribute fairly between a given number of recipients. This is one	 sequence because each number is one less than the one before. I have placed all the purple counters in this set because they are all the same colour. I will share the crayons equally

Side	A straight line that forms part of	This shape has four straight
	the boundary of a shape.	sides.
Size	An element's overall dimensions or magnitude.	The size of my shoe is smaller than my teacher's.
Sort	To organise a set of elements into specified categories.	I will sort these objects based on their size.
Square	A quadrilateral with four equal length sides and four right angles.	
Straight	A line or movement uniform in direction, without bends or curves.	The walls of the school are straight.
Subtract	Carry out the process of subtraction.	Nine subtract three is equal to six.
Subtraction	The inverse operation to addition.	We are taking some away so it is a subtraction question.
Sum	The result of one or more additions.	The sum of five and three is eight.
Surface	An outer boundary of a 3-D object.	This cone has a curved surface .
Take away	Used in the reduction structure of subtraction. To remove a number of items from a set.	He ate three of the sweets so we need to take away three counters.
Tall		Our class teacher is not as tall as our head teacher
Time	Related to duration. Measured in seconds, minutes, hours, days, weeks, months, years etc.	After lunch it will be time for P.E.
Total	The sum found by adding.	There are a total of five people at this table.
Triangle	A polygon with three sides.	
Venn diagram	Two or more circles which represent given sets and intersect according these.	blue shapes squares
Vertex (pl. vertices)	The point at which two or more lines intersect.	This shape has five vertices .
Weight	The force exerted on an object by gravity. Weight therefore changes with a change in gravitational force. Used interchangeably with mass until KS2.	The weight of this book is heavier than the pencil.

Zero	The number before one. It is	Zero comes before one on the
	neither positive nor negative.	number track.

YEAR 1		
Year 1	Definition	Example
Analogue clock	A clock with a face and hands.	
Anticlockwise	Movement in the opposite direction to the motion of the hands of a clock.	\mathbf{O}
Approximate	The number is not exact but it is close.	Our PSHE lesson lasts approximately half an hour.
Array	An arrangement of counters or numbers, in columns and rows, used to represent multiplication and division	This array shows 3 × 4, 4 × 3, 12 ÷ 4 and 12 ÷ 3
Block graph	The pre-cursor to the bar graph, this representation of data has an x- and y-axis and one block represents one item. Each block is adjoined to the adjacent block.	How children travel to school
Chart	A table or graph.	I will mark one day for the sun on our weather chart .
Chronological	In time order.	I ordered the events in my day chronologically. I woke up, ate my breakfast, went to school then came home.
Clockwise	Movement in the direction of the hands of a clock.	C
Cone	A 3-D shape with one circular plane face, which tapers to an apex.	
Continuous surface	An outer boundary of a 3-D object which is uninterrupted by any plane surfaces.	A sphere has a continuous surface .

	Quantitative information	This block graph shows us
	which has been counted o	data for the colour of the cars in
	measured.	the car park.
Decreasing	Becoming smaller in value.	15, 14, 13, 12. This number
	Used in relation to number	pattern is decreasing by one each
	sequences.	time.
Diagram	An illustration, drawing or	I will draw a diagram to show
	representation.	how I programed my floor toy
		to move.
Digit	One of the ten Arabic numerals	The number 54 has the digit five in
- 0.1	0 to 9, from which we compose	the tens column and the digit four
	numbers.	in the ones. The
		digit five has a value of fifty.
Divide	To share or group into equal	I can divide 12 by three using
	parts.	grouping or sharing.
Estimate	An appropriately accurate	I estimate there are eight
	guess, depending on the	cubes in the cup because it
	context and numbers	looks about double four but
	involved.	fewer than ten.
Even number	A number with a 0, 2, 4, 6 or 8	32 is an even number .
	in the ones and therefore	
	exactly divisible by two.	
Facts	Related to the four operations (+,	Number bonds to and within 10
	-, ×, ÷). Pupils should be	and 20 are facts , e.g. 3 + 7
	supported in achieving	= 10.
	fluency, i.e. very fast recall, in	
	these facts. These then	
	become known facts .	
Fraction	A part of a whole number,	I have shared my sweets into four
	quantity or shape.	equal parts. Everyone will get a
	Expressing a division	fraction of the whole quantity of
	relationship between two	sweets. One group is a quarter of
	integers in the	the whole.
	form .	
Half turn	A 180 degree rotation, i.e. ¹ of	
	a 360 degree or 'full' turn.	
Hour	A unit of time.	There are 24 hours in one day.
Increasing	Becoming greater in value.	2, 4, 6, 8. This number pattern is
0	Used in relation to number	increasing by two each
1	sequences.	time.
Kilogram	A standard unit of mass, equal to	

Known fact	A number fact which has been	When I use the 'Make ten'
Kilowii lact	committed to memory (or very fast recall) and can be applied fluently to various calculation	strategy to add, I use known facts to partition the number I'm
l oft	strategies.	Make a guartar turn laft and
Left	Indicating the position or direction.	Make a quarter turn left and walk forward three steps.
Litre	A standard unit of volume, equal t 1000 millilitres.	about half a litre .
Mental calculation	using a formal written strategy.	: 14 plus 5 is equal to 19. I completed this using a mental calculation and deriving facts because I know that four plus five is equal to nine.
Metre	A standard unit of measure, equal to 100 centimetres.	I estimate that the table is about a metre tall.
Minute	A unit of time.	We will have lunch in five minutes.
Oblong	A quadrilateral with two pairs of parallel sides of equal length.	
Odd number	An integer which is not divisible by two without a remainder.	All numbers which end in 1, 3, 5, 7 and 9 are odd numbers .
Partition	To split a number into two or more parts.	The number 23 can be canonically partitioned (by place value) into 20 and 3, or non-canonically partitioned in many different ways, including 18 and 5, 17 and 6, etc.

Place value	A system for writing numbers, in	In the number 452 written in
	which the value of a digit is defined by its position within the number.	base ten, the digit four has a
Position	Location, expressed either descriptively using positional prepositions, or specified by coordinates.	The book is on the table. The clock is hanging above the board.
Pound (sterling)	The official currency of the United Kingdom.	Pounds sterling are written using the <u>f</u> symbol. There are 100 pence in one pound sterling.
Property	Any attribute.	A property of a triangle is that it has three straight sides and three vertices, the sum of whose angles is 180 degrees.
Pyramid	A 3-D shape with a polygonal base and otherwise triangular faces, which form edges with the base, and which meet at an apex.	apex base
Quantity	An amount, in some cases given a numerical value.	A quantity of apples is placed on the left-hand side of the balance. How many kilogram masses will we need to place on the right to balance the apples?
Quarter	One of four equal parts of a whole, quantity or object.	I have shared the eight conkers into four equal groups – I have two conkers, which is one quarter of the whole.
Quarter turn	A 90-degree rotation, i.e. ¹ of 4 a 360 degree 'full' turn.	
Repeated addition	A structure of multiplication where equal parts are added to make a whole.	I can show 4 × 5 as repeated addition: 4 + 4 + 4 + 4 + 4.
Repeated subtraction	A structure of division, where equal parts are subtracted and the number of equal parts summed to calculate a quotient.	I can use repeated subtraction to calculate 20 divided by four: $20 - 4 - 4 - 4 - 4 - 4$
Represent	To express or show a mathematical concept using words, numerals and symbols, pictures, diagrams, or concrete manipulatives.	represent the three oranges in

		question.
Right	Indicating the position or direction.	The plidture is on the right -hand side of the board.
Rule	A consistent pattern which	□ 2, 5, 8, 11, 14…
	allows generalisation. Awareness of a rule allows a pupil to continue a sequence or generate a related sequence.	The rule is that each number is three greater than the previous number. Therefore, the next number in this sequence will be 17.
Scales	An object used to measure mass.	The scales showed that the banana had a greater mass than the apple.
Sign	Synonymous with symbol in its mathematical context, e.g. +, -, ×, ÷, =.	20 5 = 4. What is the missing sign ?
Standard unit	A uniform measure, agreed upon as standard.	Standard units of mass include grams and kilograms. Standard units of length include centimetres, metres and kilometres.Standard units of volume and capacity include millilitres and litres.
Sphere	A 3-D shape with a continuous surface, which is at all points equidistant from its centre. It has an infinite number of flat faces and straight edges.	A bowling ball is a sphere .
Symbol	Synonymous with sign in its mathematical context, e.g. +, - , ×, ÷, =.	20 5 = 4. What is the missing symbol ?

Table	A structure organised into columns and rows, in which data can be recorded.	The information for Thursday is not yet complete on the table because it is only Wednesday.
Turn	Rotation (see half and quarter turn).	A whole turn is 360 degrees. A half turn is 180 degrees. A quarter turn is 90 degrees.
Unit	An element considered as a single entity. Ten single cubes can be grouped together to make a unit of ten. A unit of measure, which can be standard or non-standard.	unit of ten.
Volume		The bottle contains a volume of one litre but its capacity is two litres. The bottle is half full.

YEAR 2		
Year 2	Definition	Example
Angle	The amount of turn,	The angle is 60 degrees.
	measured in degrees.	
Calculate	To compute or work out	Can you calculate the
	mathematically.	answer to 13 + 4?
Centimetre	A metric unit of length.	The book is 15 centimetres
		long.
Column	A vertical arrangement	of23 has two tens – I will place
	numbers or objects.	them into the tens column .
Commutative	A property of addition and	4 + 6 = 10
	multiplication. It does not	
	matter in which order the	this demonstrates that dualition
	addends or factors are added or	
	multiplied; the result will be the	
	same.	of multiplication, i.e. $3 \times 4 = 4 \times x3$
Consecutive	Following in order.	2, 3, 4, 5, 6 are consecutive
		numbers. 3, 6 and 9 are
		consecutive multiples of 3.
Denominator	The number written below the	
	vinculum in a fraction. In a	
	measure context, it indicates the	
	number of equal parts into whicl	
	the whole is divided. In a division	n
	context, it is the divisor.	
Division	The process of partitioning a	12 divided by 3 is equal to 4.
	whole into equal parts.	
Efficient	5	n I will use my number bonds
		y knowledge to calculate 22 + 7
		e efficiently . I know that 2 + 7 is
		ill equal to 9, so the answer is
	normally utilise 'known facts'.	29. That's more efficient that
_		counting on seven.
Frequency	The number of times	4 pupils have brown hair. The
	something occurs within a	frequency of brown hair is 4.
	data set.	
Gram	A metric unit of mass.	The pencil weighs 20 grams.
Heptagon	A polygon with seven sides	
	and seven angles.	
Hexagon	A polygon with six sides and six	
	angles.	
Inverse operations	Opposite operations that	Addition and subtraction are
	'undo' each other.	inverse operations.
Millilitre	A metric unit of capacity/volume	. The can of fizzy drink has a
		capacity of 330 millilitres.

Multiple	The result of multiplying a number 36 is a multiple of three
	by an integer, for example, 12 is abecause three multiplied by 12
	multiple of 3 and 4 because $3 \times 4 =$ is equal to 36. It is also a
	12. multiple of 12 for the same
	reason (and 1, 2, 4, 6, 9, 18 and
	36)

Multiplication	One of the four mathematical operations. Multiplication can be understood as repeated addition	The multiplication symbol is ×.
	or scaling (introduced in Year 3).	
Multiply	To increase a quantity by a given scale factor.	I can multiply 3 by 4 which is equal to 12.
Near double	When two numbers involved in an addition are close in value, such as 23 + 22. The numbers can be treated as exact doubles, followed by compensating.	To calculate 23 + 22, I can use the near double strategy. I can double 22 and then add one more.
Non-unit fraction	A fraction with a numerator greater than one.	Two thirds is a non-unit fraction.
Numerator	The number written above the vinculum in a fraction. In a measure context, it indicates the specified number of parts out of the whole. In a division context, it is the dividend.	In the fraction one quarter, one is the numerator .
Octagon	A polygon with eight sides and eight angles.	
Operation	A mathematical process. The fou mathematical operations are addition, subtraction, multiplication and division.	r 4 + 2 = 6. The operation is eaddition.
Pentagon	A polygon with five sides and five angles.	
Pictogram	A representation of data using pictures or symbols.	Countries people visited

Quadrilateral	A 2D shape with four sides and four angles. which add up to 360 degrees.
Relationship	The way in which two or more The relationship between things are connected. addition and subtraction is that they are the inverse of each other.
Right angle	An angle of 90 degrees. A square has four right angles.
Rotation	The act of rotating about an axis/centre.
Scale	Equally spaced markings on aUsing the scale on the ruler, th
	measuring device which can bebook measures 15cm. read to quantify a measurement.
Symmetry	A shape is symmetrical when it fits triangle has one line of fits exactly onto itself when folded in half.

Tally	A form of counting. Each tally is a Four children have black hair; I vertical mark. After the fourth will record this as four tallies . vertical mark, a fifth horizontal/diagonal mark is drawn to create a group of five.
Temperature	The measure of heat. Outside has a temperature of 15 degrees Celsius.
Unit fraction	A fraction with a numerator of One-third is a unit fraction . one.
Vinculum	A horizontal line that separates 1 the numerator and the denominator in a fraction.

YEAR 3		
Year 3	Definition	Example
Acute angle	An angle that is smaller than a right angle.	It is smaller than my right angle checker so this must be an acute angle.
Axis (plural: axes)	A real or imaginary reference line. The y-axis (vertical) and x-axis (horizontal) on charts and graphs are used to show the measuring scale or labels for the variables.	The y- axis on this bar graph shows you how many pupils preferred each colour.
Bar graph	A representation of data in which the frequencies are represented by the height or length of the bars.	This bar graph shows us the preferred colours of the pupils in our Year 3 class.
Columnar addition/subtraction	The formal written algorithms for addition and subtraction that are exemplified in <i>Mathematics Appendix 1</i> of the 2014 national curriculum.	Solve the following calculations by using the appropriate method of columnar addition or subtraction .
Factor	A number, that when multiplied with one or more other factors, makes a given number.	The number six has four factors : 1, 2, 3 and 6.
Formal written methods		Pupils should only use formal written methods for calculations that cannot be efficiently calculated using mental strategies (with or without jottings).
Horizontal	Horizontal refers to planes and line segments that are parallel to the horizon.	The x-axis on a graph should be horizontal .
Irregular	In geometry, irregular is a term used to describe shapes that are not regular (see below).	The sides and the angles of this pentagon are not all equal so the pentag <mark>on is irregular</mark> .
Kilometre	A metric unit measure of length that is equal to one thousand metres.	The distance from the school to Arun's house was exactly one kilometre .
Millimetre	A metric unit measure of length that is equal to one thousandth of one metre.	The length of Philippa's ruler is 300 millimetre s.
Numeral	A numeral is a symbol (or group of symbols) used to represent a number.	Whole numbers can all be represented as numerals consisting of the digits 0 to 9.

Obtuse angle	An angle that is greater than a right angle but less than 180	It is greater than my right angle checker so this angle
	degrees.	must be obtuse .
Parallel	Line segments that can be described as parallel must be or the same plane and will neve meet, regardless of how far eithe or both line segments are extended.	r
Perimeter	The perimeter of a 2-D shape is the total distance around its exterior.	I know that one side of this square is 2cm so it must have a perimeter of 8cm.
Perpendicular	A pair of line segments (or surfaces) can be described as perpendicular if they intersect at (or form) a right angle.	The adjacent sides of a rectangle are perpendicular .
Place holder	any place value column (that	I need to use a place holder in the ones column to make it clear that my number is 320 and not 32.
Prism	A prism is a 3-D solid with two identical, parallel bases and otherwise rectangular faces.	A triangular prism has five faces, consisting of three rectangles and two triangles which are parallel.
Product	The result you get when you multiply two numbers.	24 is the product of 3 and 8.
Regular	Regular 2-D shapes (regula polygons) have angles that are all equal and side lengths that are all equal.	rA square is a regular 2-D shape because all four angles are right angles and all four sides are the same length. A cube is a regular 3-D shape with six identical square faces.
Roman numeral	Roman numerals are a system of symbols used to represent numbers that were developed and used by the Romans. They do not use a place value system.	clock is represented by the Roman numerals XII, which is
Round	Approximate a number, normally to the nearest multiple of ten, to make it easier with which to calculate.	I would round the number 17 to 20 because it is three away from 20 but seven away from 10.

	A pyramid is a 3-D shape with a 2-D shape (which gives the pyramid its name) as a base and triangular faces that taper to a	five faces; one square face and
Triangle-based pyramid		This triangle-based pyramid has four triangular faces.

YEAR 4		
Year 4	Definition	Example
Area	The space a surface takes up inside its perimeter. Area is always measured in square units.	The area is 8 square units.
Associative law	No matter how the parts in an addition or multiplication equation are grouped, the answer will be the same.	(6 + 3) + 2 = 11 6 + (3 + 2) = 11 Addition and multiplication are associative . Subtraction and division are not.
Convert	To change from one unit of measurement to another.	2 km can be converted to metres – it is equal to 2000 m.
Coordinate	The position of a point, usually described using pairs of numbers. Sometimes called Cartesiar coordinates, after the mathematician Rene Descartes.	
Decimal fraction	A fraction expressed in its decimal form.	Half written as a decimal fraction is 0.5.
Distributive law	The process whereby adding some numbers and then multiplying the sum gives the same answer as multiplying the numbers separately and then adding the products.	3 × 12 = (3 × 10) + (3 × 2)

Dividend	The amount that you want	In '12 ÷ 3 = 4', 12 is the
	to divide.	dividend.
Divisor	The number you divide by.	In '12 ÷ 3 = 4', 3 is the divisor .
Equilateral	Having all sides the same length.	An equilateral triangle has three equal sides.
Equivalent	Equivalent means having the same value. Equivalent fractions have the same value.	2 = 1 4 2
Expression	One or a group of numbers, symbols or operators. An expression does not use equality or inequality signs. Using an equality or inequality sign will give an equation.	4 ²
Grid	A series of evenly divided and equally spaced shapes, usually squares.	
Improper fraction	A fraction where the numerator is bigger than the denominator. These fractions are therefore greate than one whole.	12 11 r
Integer	A whole number that can be positive or negative.	6 is an integer, 0.6 is not.
Interval	An interval on a graph's axis lies between two values.	If one point on an axis is 50 and the next 60, the interval is 10.
lsosceles	Having two sides of equal length. Isosceles triangles have two equal sides; isosceles trapezia have two equal, non-parallel sides.	
Kite	A 2-D shape with two pairs of equal length adjacent sides. The diagonals intersect at right angles.	
Line graph	A graph that uses lines to connect the points on a data chart. Used to present continuous data, such as change over time.	Temperature graph
Mixed numbers	Numbers consisting of an integer and fractional part.	$\frac{1}{2}$ $\frac{1}{3}$ $\frac{3}{4}$

Negative number	A number that is less than	-1, -24, -o.5 etc.
5	zero. (It is helpful to refer	
	to these numbers as	
	'negative numbers' rather	
	than 'minus' to avoid	
	confusion with the operation	
	'minus'.)	

l

Parallelogram	A 2-D shape that has two pair of parallel sides and equal opposite angles.	's
Plot	To mark out a point on a graph or grid.	'Plot the point (3,6)' means to draw the precise location of that point, usually shown as a dot or a small cross.
Point	The precise location of a position on a 2-D plane.	An exact place on a graph or on squared paper. A point is often represented by a capital letter.
Positive number	A number that is greater than zero. Zero is neither positive or negative.	3, 32, 0.5
Proper fraction	A fraction with a value less than one.	1 3 5 2′4′8
Protractor	A measuring device for measuring the size of an angle. Angles are measured in degrees (°).	
Quotient	The result when the dividend is divided by the divisor.	15 ÷ 3 = 5 5 is the quotient .
Rectilinear	-	A rectangle. A straight-sided shape that can be divided up into other rectangles.
Rhombus	An equilateral parallelogran with four equal length sides.	n
Scalene	A scalene triangle has three unequal sides and three unequal angles.	
Short division	A formal written layout where the quotient is calculated showing only one written step.	<u>77</u> 5385
Short multiplication	A formal written layout where the multiplier is usually 9 or less.	782 <u>× 9</u> 7038
Simplify	To write a number or equation in its simplest form.	I can simplify ⁸ to ⁴ . 10 5

	equal to a square with the	Sometimes referred to as centimetre squared, abbreviated to cm² .
Trapezium	A quadrilateral with exactly one pair of parallel sides.	

YEAR 5		
Year 5	Definition	Example
Angle at a point	Angles that meet at a point that sum to 360°.	$ \begin{array}{c} 110^{\circ} \\ 50^{\circ} \\ a^{\circ} \\ 125^{\circ} \\ b^{\circ} \end{array} $
Angle on a line	Angles formed on a straight line that sum to 180°.	2
Average (mean)	A measure of central tendency. The mean average of a set of data is the sum of the quantities divided by the number of quantities.	÷ 4 = 5.
Common factor	A factor of two (or more) given numbers.	A common factor of 12 and 9 is 3 because $3 \times 4 = 12$ and $3 \times 3 = 12$.
Common multiple	A multiple of two (or more) given numbers.	A common multiple of 3 and 6 is 12 because $3 \times 4 = 12$ and $6 \times 2 = 12$.
Congruent		The two triangles are congruent . If I place one on top of the other, there is no overlap.
Cube number	The product of three equal factors.	Eight is a cube number because $8 = 2$ × 2 × 2 = 2^3 .
Cubic centimetre	The space taken up by a cube with edges of length 1 cm of which measures 1 cm × 1 cm > 1cm.	r <
Cubic metre	A unit used to measure volume. The space taken up by a cube with edges of length 1 metre.	The volume of this fridge is two cubic metres.
Decagon	A polygon with ten sides and ten angles.	$\sum_{i=1}^{n}$
Degree	The unit of measure for angles.	A right angle is 90 degree s.

Diagonal	A straight line segment that joins one vertex to another.	The diagonals of a kite ars Perpendicular
Divisible	A number is said to be divisible by another if it can be divided by that number without a remainder.	24 is divisible by 8. When divided by 8 it gives a quotient of 3, with no remainder.
Dodecagon	A polygon with twelve sides and twelve angles.	
Long division	The formal written algorithm that can be used to divide by a number with two or more digits.	$ \begin{array}{c c} 3 4 \\ 12 \overline{408} \\ \underline{36} \\ 4 8 \\ \underline{48} \\ 0 \end{array} $
Long multiplication	The formal written algorithm that can be used to multiply a number by a number with two or more digits.	$ \begin{array}{r} 3 \ 4 \\ \times \ 1 \ 2 \\ \hline 6 \ 8 \\ \hline 3 \ 4 \ 0 \\ \hline 4 \ 0 \ 8 \end{array} $
Negative integer	A whole number with a value less than zero. Zero is neither positive nor negative.	When the temperature falls below 0° a negative integer is used to record it.
Nonagon	A polygon with nine sides and nine angles.	OR
Percentage	The number of parts per hundred which is written using the % symbol.	30% means for every 100 there are 30.
Polygon	A 2-D shape with three or more straight sides.	Triangles and rectangles are examples of polygons .
Polyhedron (pl. polyhedra)	A 3-D shape with flat surfaces that are polygons.	A cuboid is a polyhedron . A cylinder is not a polyhedron because it has a curved surface.
Prime factor	A factor that is a prime number.	3 and 2 are prime factors of 6.
Prime number	A whole number with only two factors, one and the number itself.	2, 3, 5, 7, 11, 13, 17 and 19 are the prime numbers less than 20.

Remainder	The amount remaining after	21 divided by four is equal to five with
Remainaei	division when a whole number	
	answer is needed.	
Reflection	A mirror image that is	The shape has been reflected in the
	equidistant from a mirror line.	dotted mirror line.
Reflex angle	An angle that is greater than 180°.	$\sum_{i=1}^{n}$
Scale (not to scale)	The ratio of lengths, in a drawing, are in proportion to the measurements of the real object. The lengths are not in proportion when not to scale.	The diagram was not drawn to scale . That means I can't use a ruler to measure the sides, because they are not in proportion to the real object.
Square metre	A unit of measure for area. The surface covered by a square with sides of length one metre.	The area of the floor in a room might be measured in square metres .
Square number	The product of two equal factors.	9 is a square number because $9 = 3 \times 3 = 3^2$.
Tetrahedron	A 3-D shape with four triangular faces.	
Transformation	A collective term for the ways that shapes can be changed, resulting in congruent or similar shapes, i.e. translation, reflection, rotation or enlargement.	, types of transformations .

Translation	When a shape moves so that it Triangle C has been translated three is in a different position but right and two down resulting in retains the same size, area, triangle D.
	angles and side length and so is congruent.

YEAR 6		
Year 6	Definition	Example
Arc	A portion of the circumference o a circle	•
Brackets	The symbols () used to separate parts of a multi-step calculation.	(10 – 2) × 3 = 21
Centre		To draw a circle, I place the point of my pair of compasses at the centre .
Circumference	The perimeter/boundary of a circle.	
Compasses	A tool for creating curved lines, arcs and circles.	I can use a pair of compasses to draw a circle with a radius of 4 cm.
Common fraction	A fraction written with a numerator and denominato separated by a vinculum.	One quarter can be written as ra common fraction,.
Degree of accuracy	A description of how accurately a value is communicated.	The degree of accuracy needed for the answer is one decimal place.
Diameter	A line from one point of the circumference of a circle to another on the opposite side, which must pass through the centre of the circle.	The circumference of a circle is the diameter multiplied by pi.
Equivalent expression	An expression, which can be algebraic, which is equal in value to another expression.	Find an equivalent expression to 17 + 10. 18 + 9 is an equivalent expression to 17 + 10.
Factorise	To identify factors of a given number. To express a number as factors.	I can factorise 12 by looking at its factor pairs. $1 \times 12 = 12$, $2 \times 6 = 12$, $3 \times 4 = 12$. So the factors of 12 are 1, 2, 3, 4, 6 and 12.
Foot/feet	An imperial unit of measure of length.	I am approximately five feet tall.
Formula	An algebraic expression of a rule.	The area of a rectangle can be found by multiplying the width and height. a = w × h
Gallon	An imperial unit of measure of volume/capacity.	A gallon is approximately 4.5 litres

used in the UK but is now used less often, except in the context	Miles are an imperial unit to measure length.
of length. Includes miles, pounds and pints.	

Inch	An imperial unit of measure.	An inch is approximately 2.2 cm.
Intersect	The point at which two (or more) lines meet is where they intersect.	The x and y axes intersect at (0,0)
Metric unit	A standard unit of measure used in the UK and Europe. Includes centimetres, litres and kilograms.	Litres are a metric unit used to measure volume.
Mile	An imperial unit of measure of length.	Five miles is equivalent to eight kilometres.
Net	A group of 2-D shapes which, when folded and connected, forms a 3-D polyhedron.	The net of a cube is comprised of six connected squares.
Order of operations	The internationally agreed order to complete operations in a multi-step equation with multiple operations.	$(3 + 4) \times 2 = \Box$ The order of operations dictates that the operation within the brackets is completed first.
Origin	The point at which axes in a coordinates grid cross; the point (0,0).	s indicated by the blue dot.
Ounce	An imperial unit of measure of mass.	The newborn baby had a mass of 6 pounds and 3 ounces .
Pie chart	A representation of a set of data where each segment represents one group in proportion to the whole.	Nationality of Astronauts on Board ISS January 2017
		Russia USA France
Pint	An imperial unit of measure.	I found a pint of milk on my doorstep.
Pound (mass)	An imperial unit of measure of mass.	The new-born baby had a mass of 6 pounds and 3 ounces.

Proportion	A comparison between two or Two thirds of a class were boys.
	more parts of a whole or group. The proportion of the class that
	Proportion expresses a is girls is one third.
	part-whole relationship. This may
	be represented as a fraction, a
	percentage or a decimal.

Quadrant	One of four regions into which a coordinates grid is divided.	Second Quadrant Negative x, positive y First Quadrant Positive x and y values Third Quadrant Negative x, negative y Fourth Quadrant Positive x, negative y
Radius	A line from one point of the circumference of a circle to the centre of the circle.	
Ratio		
Similar	Similar shapes are those which have the same internal angles and where the side lengths are in the same ratio or proportion. Enlarging a shape by a scale factor (for example by doubling all side lengths) creates a similar shape.	another.
Square millimetre	The area of a square with sides 1 mm.	The smallest squares on graph paper have an area of one square millimetre.
Square kilometre	The area of a square with sides 1 km.	The area of England is 130 279 square kilometres.

Vertically opposite angles	Angles which are positioned opposite to one another when two lines intersect.
	The purple angles indicated are vertically opposite angles.